

CERTAIN TRANSFORMATION FORMULAS FOR BASIC HYPERGEOMETRIC SERIES

Jayprakash Yadav

Department of Mathematics and Statistics,
Prahladrai Dalmia Lions College of Commerce and Economics,
Sundar Nagar, Malad (W), Mumbai-400064, INDIA.
E-mail: jayp1975@gmail.com

Abstract: The object of this paper is to establish some transformation formulas for basic hypergeometric series by making use of some known results.

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1. Introduction

The generalized basic hyper geometric series ${}_r\phi_s$ is defined by

$${}_r\phi_s \left[\begin{matrix} a_1, a_2, \dots, a_r \\ b_1, b_2, \dots, b_s \end{matrix} ; q, z \right] = \sum_{n=0}^{\infty} \frac{(a_1, a_2, \dots, a_r)_n}{(b_1, b_2, \dots, b_s)_n} [(-1)^n q^{n(n-1)/2}]^{1+s-r} z^n \quad (1)$$

If $0 < |q| < 1$, the above series converges absolutely for all z if $r \leq s$ and for $|z| < 1$ if $r = s + 1$.

The abnormal type of generalized basic hyper geometric series ${}_r\phi_s(\cdot)$ is defined as

$${}_r\phi_s \left[\begin{matrix} a_1, a_2, \dots, a_r; q, z \\ b_1, b_2, \dots, b_s; q^\lambda \end{matrix} \right] = \sum_{n=0}^{\infty} \frac{(a_1, a_2, \dots, a_r; q)_n}{(b_1, b_2, \dots, b_s; q)_n} z^n q^{\lambda n(n+1)/2} \quad (2)$$

where $\lambda > 0$ and $|q| < 1$.

As usual, the q -shifted factorial is defined by

$$(a, q)_n = \begin{cases} 1 & \text{if } n = 0; \\ (1-a)(1-aq)(1-aq^2)\dots, (1-aq^{n-1}) & \text{if } n \in N. \end{cases} \quad (3)$$